

Learning Points and Routes to Recommend Trajectories

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1 The Problem

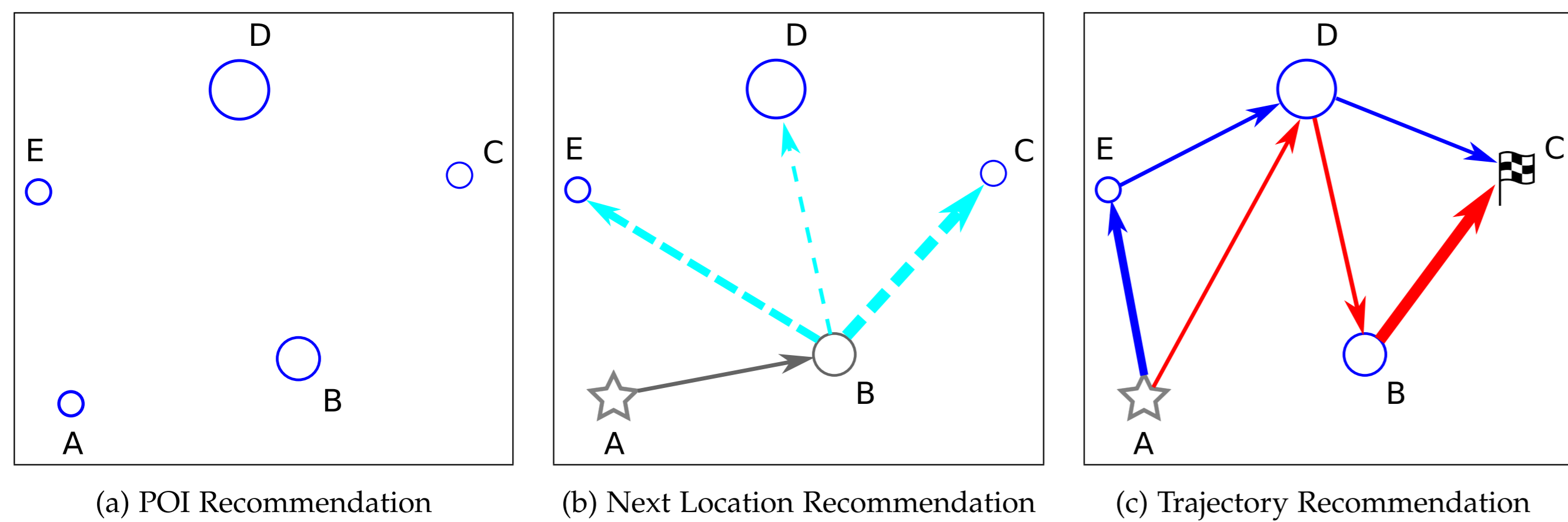


Figure 1: Three settings of trajectory recommendation problems. Instead of scoring POIs (Figure a) or recommending the next location (Figure b), we focus on recommending a whole trajectory (Figure c).

Problem formulation: given a set of POIs \mathcal{P} and a query $q = (p_s, p_e, L)$, i.e., the start/end location and the number of desired POIs, we recommend a trajectory $\mathcal{T} = (p_s, \dots, p_e)$ with L POIs.

2 Main Contributions

- Optimise point preferences and routes jointly.
- Feature-driven approach and learning from past behaviour.
- New evaluation metric that captures POI visiting orders.

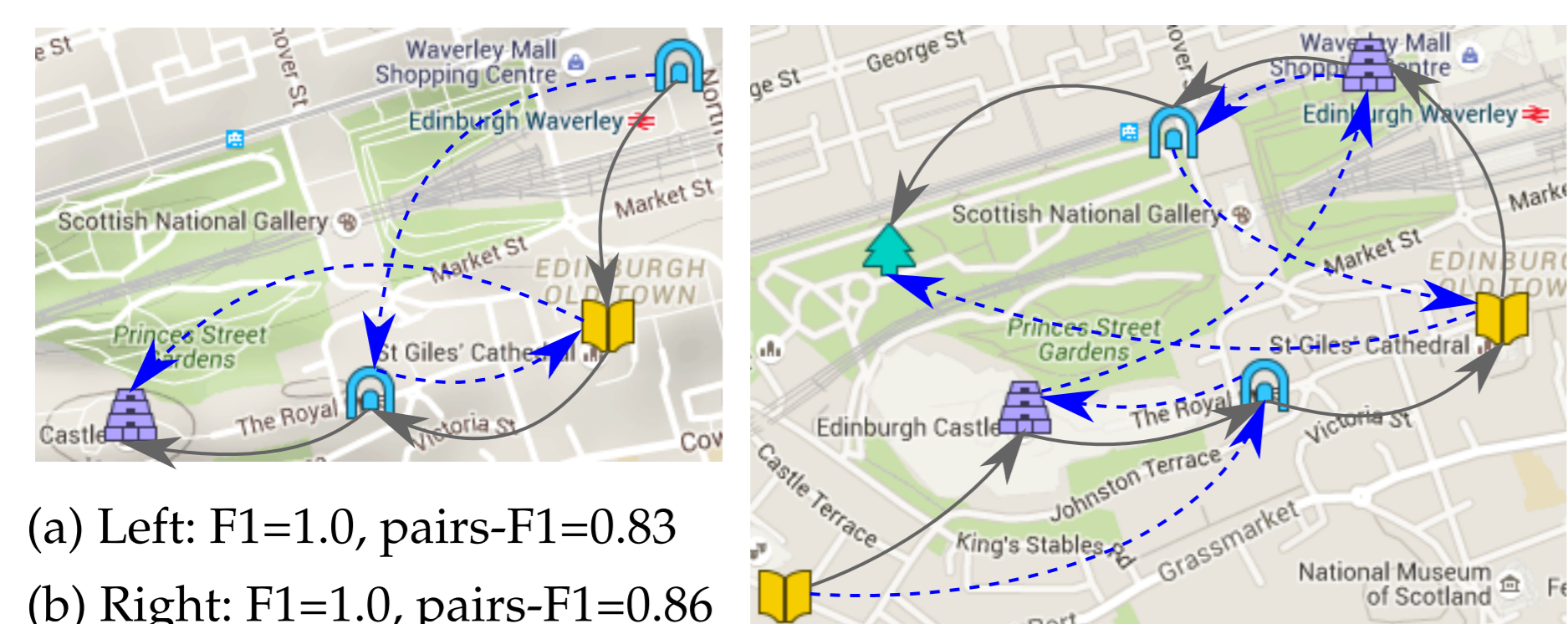


Figure 2: Examples for F_1 vs $\text{pairs-}F_1$ as evaluation metric. $\text{pairs-}F_1$ lies between 0 and 1, and achieves 1 iff two trajectories are exactly the same.

To measure the similarity between two trajectories, we propose a new metric, $\text{pairs-}F_1$, that takes into account both the point identity and the visiting orders in a trajectory. It measures the F_1 score of every pair of ordered POIs: $\text{pairs-}F_1 = 2P_{\text{PAIR}}R_{\text{PAIR}} / (P_{\text{PAIR}} + R_{\text{PAIR}})$.

3 Methods

Rank POIs using POI and query specific features via rankSVM.

$$\min_{\mathbf{w}} \frac{1}{2} \mathbf{w}^T \mathbf{w} + C \sum_{p_i, p_j \in \mathcal{P}, q_n \in \mathcal{Q}} \max(0, 1 - \mathbf{w}^T (\phi_{i,n} - \phi_{j,n}))^2.$$

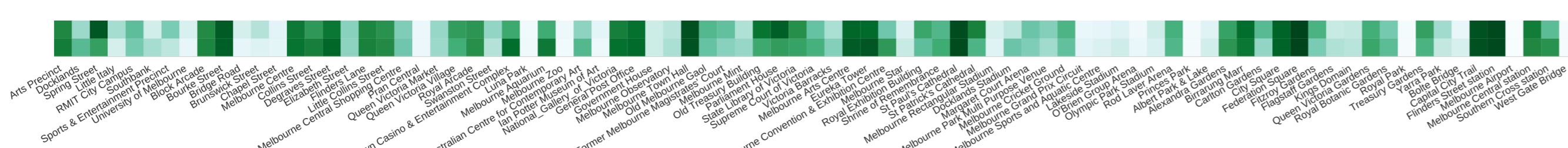


Figure 3: Examples of POI ranks in Melbourne. Top: POI ranks with respect to query ($p_s = \text{Spring Street}$, $p_e = \text{Federation Square}$, $L = 5$), the top-3 POIs are (Flinders Street station, St Paul's Cathedral, Melbourne Town Hall), the bottom-3 POIs are (Royal Park, West Gate Bridge, Melbourne Airport); Bottom: POI ranks with respect to query ($p_s = \text{Federation Square}$, $p_e = \text{Melbourne Aquarium}$, $L = 4$), the top-3 POIs are (Flinders Street station, St Paul's Cathedral, Capital City Trail), the bottom-3 POIs are (West Gate Bridge, Royal Park, Melbourne Airport).

Learn Routes

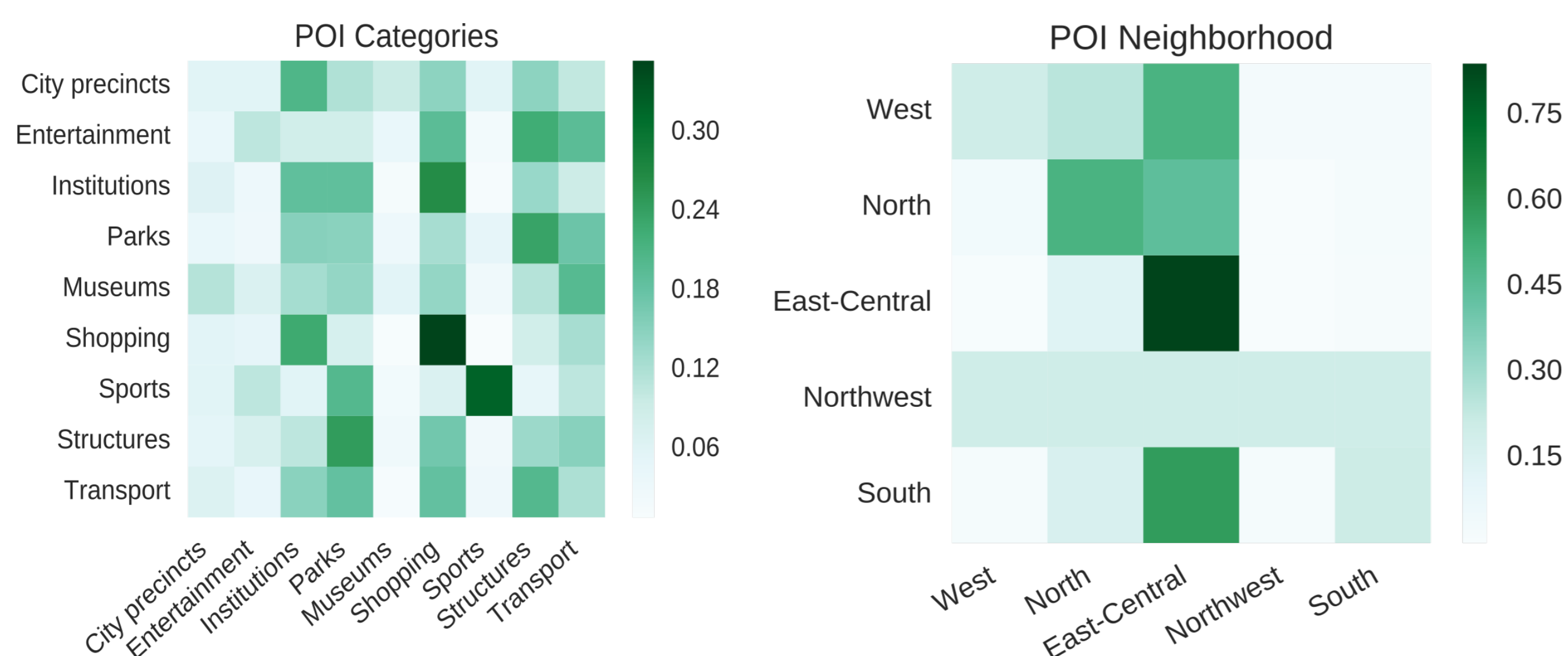


Figure 4: Model POI transitions using a Markov chain with discrete states and factorise the POI-POI transition matrix along different types of POI properties. Left: Transition matrix for POI category; Right: Transition matrix for POI neighborhood.

Combine Ranks and Routes

Maximise the ranking of POIs in trajectory as well as the transition likelihood simultaneously using Viterbi algorithm.

$$\operatorname{argmax}_{\mathcal{T} \in \mathcal{P}^L} \alpha \sum_{k=2}^L \log P_R(p_k|q) + (1 - \alpha) \sum_{k=1}^{L-1} \log P(p_{k+1}|p_k).$$

Avoid Sub-tours

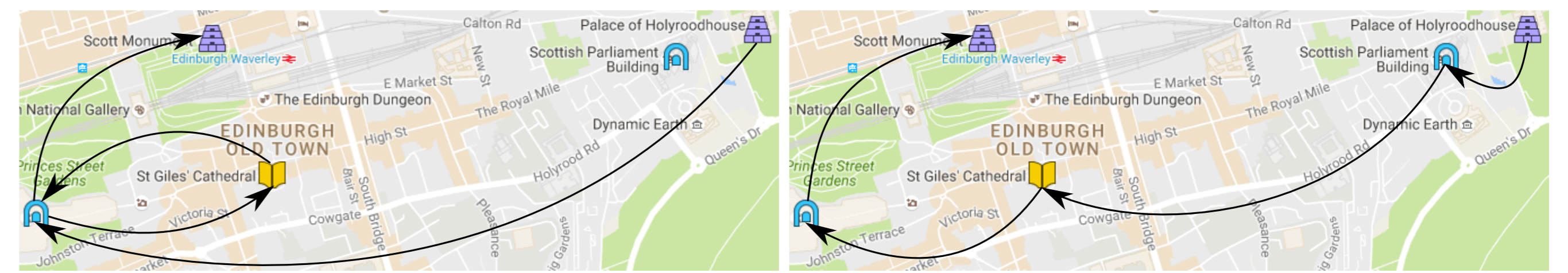


Figure 5: To avoid sub-tours in trajectories recommended by Viterbi algorithm, an integer linear program (ILP) with sub-tour elimination constraints was employed. Left: Trajectory recommended using Viterbi algorithm given a query; Right: Trajectory recommended by ILP with respect to the same query.

4 Experimental Results

	#Photos	#Visits	#Traj.	#Users
Edinburgh	82,060	33,944	5,028	1,454
Glasgow	29,019	11,434	2,227	601
Melbourne	94,142	23,995	5,106	1,000
Osaka	392,420	7,747	1,115	450
Toronto	157,505	39,419	6,057	1,395

Table 1: Dataset of trajectories extracted from Flickr photos in five cities.

	Query POI	Trans.	No sub-tours
RANDOM	×	×	×
PERS TOUR	×	✓	×
PERS TOUR-L	×	✓	✓
POI POPULARITY	×	✓	×
POI RANK	✓	✓	×
MARKOV	×	✓	×
MARKOV PATH	×	✓	✓
RANK+MARKOV	✓	✓	×
RANK+MARKOV PATH	✓	✓	✓

Table 2: Information captured by nine different trajectory recommendation algorithms.

Performance Comparison

Table 3: Performance comparison on five datasets in terms of F_1 score. The best method for each city is shown in **bold**, the second best is shown in *italic*.

	Edinburgh	Glasgow	Melbourne	Osaka	Toronto
RANDOM	0.570 ± 0.139	0.632 ± 0.123	0.558 ± 0.149	0.621 ± 0.115	0.621 ± 0.129
PERS TOUR	0.656 ± 0.223	0.801 ± 0.213	0.483 ± 0.208	0.686 ± 0.231	0.720 ± 0.215
PERS TOUR-L	0.651 ± 0.143	0.660 ± 0.102	0.576 ± 0.141	0.686 ± 0.137	0.643 ± 0.113
POI POPULARITY	0.701 ± 0.160	0.745 ± 0.166	0.620 ± 0.136	0.663 ± 0.125	0.678 ± 0.121
POI RANK	0.700 ± 0.155	0.768 ± 0.171	0.637 ± 0.142	0.745 ± 0.173	0.754 ± 0.170
MARKOV	0.645 ± 0.169	0.725 ± 0.167	0.577 ± 0.168	0.697 ± 0.150	0.669 ± 0.151
MARKOV PATH	0.678 ± 0.149	0.732 ± 0.168	0.595 ± 0.148	0.706 ± 0.150	0.688 ± 0.138
RANK+MARKOV	0.659 ± 0.174	0.754 ± 0.173	0.613 ± 0.166	0.715 ± 0.164	0.723 ± 0.185
RANK+MARKOV PATH	0.697 ± 0.152	0.762 ± 0.167	0.639 ± 0.146	0.732 ± 0.162	0.751 ± 0.170

Table 4: Performance comparison on five datasets in terms of $\text{pairs-}F_1$ score. The best method for each city is shown in **bold**, the second best is shown in *italic*.

	Edinburgh	Glasgow	Melbourne	Osaka	Toronto
RANDOM	0.261 ± 0.155	0.320 ± 0.168	0.248 ± 0.147	0.304 ± 0.142	0.310 ± 0.167
PERS TOUR	0.417 ± 0.343	0.643 ± 0.366	0.216 ± 0.265	0.468 ± 0.376	0.504 ± 0.354
PERS TOUR-L	0.359 ± 0.207	0.352 ± 0.162	0.266 ± 0.140	0.406 ± 0.238	0.333 ± 0.163
POI POPULARITY	<i>0.436 ± 0.259</i>	0.507 ± 0.298	0.316 ± 0.178	0.365 ± 0.190	0.384 ± 0.201
POI RANK	0.432 ± 0.251	<i>0.548 ± 0.311</i>	0.339 ± 0.203	0.511 ± 0.309	0.518 ± 0.296
MARKOV	0.417 ± 0.248	0.495 ± 0.296	0.288 ± 0.195	0.445 ± 0.266	0.407 ± 0.241
MARKOV PATH	0.400 ± 0.235	0.485 ± 0.293	0.294 ± 0.187	0.442 ± 0.260	0.405 ± 0.231
RANK+MARKOV	0.444 ± 0.263	0.545 ± 0.306	0.351 ± 0.220	0.486 ± 0.288	0.512 ± 0.303
RANK+MARKOV PATH	0.428 ± 0.245	0.533 ± 0.303	<i>0.344 ± 0.206</i>	0.489 ± 0.287	0.514 ± 0.297

Observations

- Learning-based approaches generally outperform heuristic route recommendation.
- Incorporating transitions to POI ranking results in a better sequence of POIs.
- Avoiding sub-tours improves performance of classical Markov chain methods.

An Illustrative Example

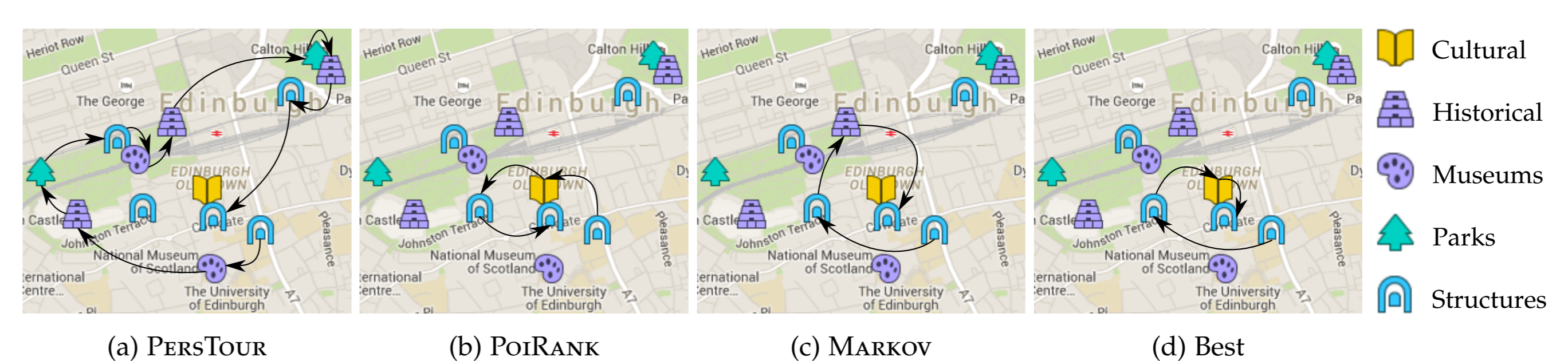


Figure 6: Example of different recommendations from algorithm variants. The best result (Figure d), with exactly the same points and routes as the ground truth, is achieved by RANK+MARKOV PATH.